

Zumdahl Chapter 7

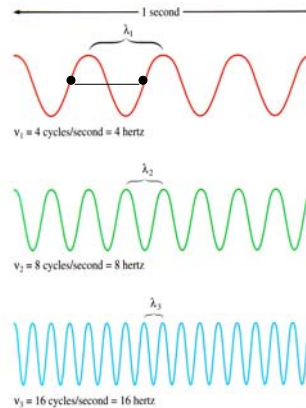
Atomic Structure and Periodicity

1. The nature and properties of waves:

- Wavelength \equiv distance between two peaks or troughs. (λ)
- Frequency \equiv number of cycles that pass through a given point in space per unit time. (ν)

$$\nu = \frac{\text{distance travelled/second}}{\text{distance/cycle}}$$

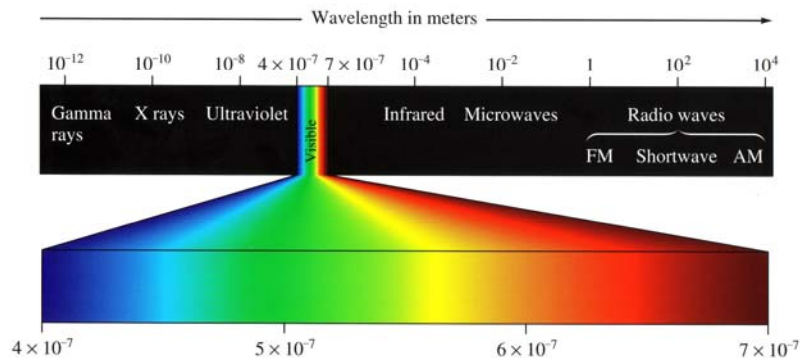
$$= \frac{\text{speed}}{\text{wavelength}} = \frac{\nu}{\lambda} \quad \frac{(m/s)}{m} \equiv s^{-1} \text{ or Hz}$$



- Light \equiv **electromagnetic** radiation (how energy “travels” through space)
- Radiation \equiv emission and transmission of energy in the form of waves

Magnetic and Electric fields

- For all electromagnetic radiation, speed $c = 2.998 \times 10^8 \text{ m/s}$



- For an electromagnetic wave:

$$\nu = \frac{c}{\lambda}$$

WHY? Interaction between matter and electromagnetic radiation \equiv **SPECTROSCOPY** \longrightarrow information about atoms, molecules and structure.

2. The nature of matter

- **Before 1900:**
 - matter \equiv particles
 - light \equiv electromagnetic radiation (waves)
- **Beginning of the 20th century:** discovery of *phenomena* that could not be explained by classical physics: Blackbody radiation, photoelectric effect, Compton effect, atomic and molecular spectra, etc.. could be explained only by a modern view: development of **QUANTUM THEORY**

- **Planck (1900):** energy can be gained or lost only in whole numbers of the quantity $h\nu$, where

ν \equiv frequency of the electromagnetic radiation absorbed or emitted.

$$\Delta E = n h \nu$$

$$n = 1, 2, 3, \dots$$

$$h = 6.626 \times 10^{-34} \text{ J s}$$

Planck's constant

$h\nu$ \equiv a discrete package of energy or **quantum** \Rightarrow energy is **quantized**.

- **Einstein (1905):** "special theory of relativity"

$$E = mc^2 \Rightarrow m = E/c^2 \dots \text{energy has mass!}$$

Einstein (1905): “The photoelectric effect”

When a metal is irradiated with light, electrons are ejected from its surface → generation of a **photocurrent**.

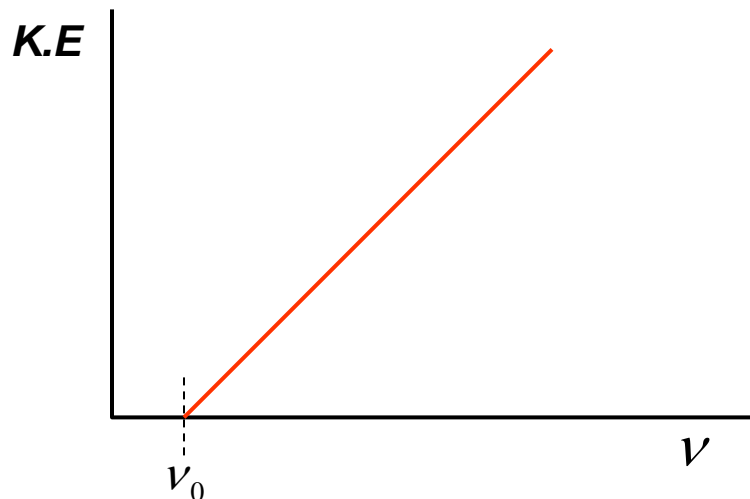
1. No electrons are emitted unless the frequency of the incident light exceeds a minimum frequency (threshold): $\nu > \nu_0$.
2. For light with frequency less than the threshold, no electrons are emitted, regardless of the intensity of the light.
3. If $\nu > \nu_0$, the number of electrons emitted increases with the intensity of the light.
4. If $\nu > \nu_0$, the kinetic energy (K.E) of the emitted electrons increases linearly with the frequency of the light.

$$h\nu = h\nu_0 + K.E$$

$E_0 = \text{Work function}$

$$\equiv E_0 + \frac{1}{2}mv^2$$

Photoelectric effect

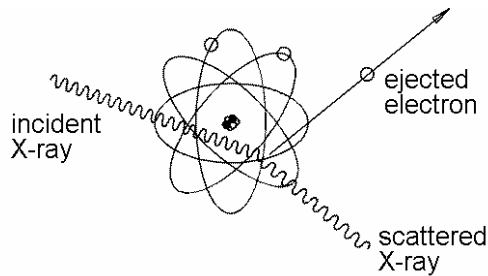


The kinetic energy of the electron increases linearly with ν . Note that the kinetic energy **cannot go negative**.

In the photoelectric effect: Einstein assumed the electromagnetic radiation itself to be quantized:

existence of “**particles of light**” or **photons**

- **Does a photon have mass??**
- **Compton (1922):** The collision of X-rays with electrons:



photons exhibit the mass calculated from the equation:

$$m = \frac{h}{\lambda c}$$

Rationalization:

$$\left\{ \begin{array}{l} E = mc^2 \\ = h \frac{c}{\lambda} \end{array} \right. \Rightarrow m = \frac{h}{\lambda c} \quad \text{Dual nature of light: light manifests itself as particles}$$

- **Conversely, does matter possess wave properties??**
- **De Broglie (1923):** Every particle is associated with a wave of wavelength:

$$\lambda = \frac{h}{mv}$$

De Broglie's wavelength

Do sample exercises 7.1, 7.2, 7.3

Electron: $\left\{ \begin{array}{l} m_e = 9.11 \times 10^{-31} \text{ kg} \\ v_e = 1.0 \times 10^7 \text{ m/s} \end{array} \right. \quad \left| \Rightarrow \lambda_e = 7.3 \times 10^{-11} \text{ m} \right.$

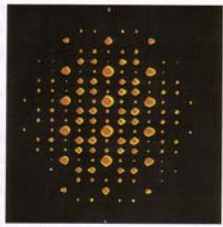
Ball: $\left\{ \begin{array}{l} m_b = 0.10 \text{ kg} \\ v_b = 35 \text{ m/s} \end{array} \right. \quad \left| \Rightarrow \lambda_b = 1.9 \times 10^{-34} \text{ m} \right. \text{ !!}$

▪ **DIFFRACTION**

Separation of the light into rays of different wavelengths, as it is scattered from a regular array of points or lines:

- spectrum of colors obtained as light is reflected from the grooves of a compact disk.
- shades of colors observed as light passes through a prism.

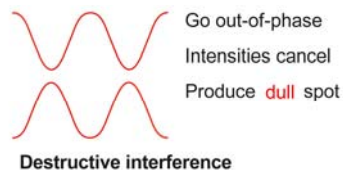
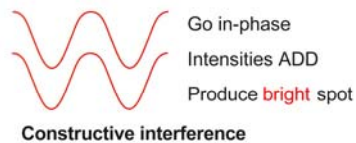
A crystal of NaCl (array of Na⁺ Cl⁻ Na⁺ Cl⁻ ...) also produces a **DIFFRACTION PATTERN** upon interaction with X-rays.



Diffraction pattern of a Ti-Ni alloy

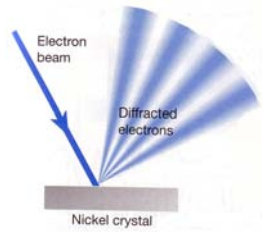
The diffraction pattern can only be explained in terms of interference of waves.

Recall: $\lambda_e \cong 10^{-10} \text{ m}$ (1 Å)
 \Rightarrow typically the distance between the ions in an NaCl crystal.



Hence, a crystal should be able to diffract electrons as well !

- **Davisson and Germer (1927)**



Electrons are diffracted from the Ni crystal, just like X-rays !

De Broglie's hypothesis is thus justified.

Wave and particle nature of matter melt together:

The **WAVE PARTICLE DUALITY**